

n being a composite number formed from the product of $p_1 \cdot p_2 \cdot \dots \cdot p_k$ where k is an integer greater than 2, p_1, p_2, \dots, p_k are distinct prime numbers, and where C is a number representative of an encoded form of message word M, wherein said encoding step comprises the step of:

transforming said message word signal M to said ciphertext word signal C whereby

$$\begin{aligned}C_1 &= M_1^{e_1} \bmod p_1 \\C_2 &= M_2^{e_2} \bmod p_2 \\&\vdots \\C_n &= M_n^{e_n} \bmod p_n\end{aligned}$$

$$\begin{aligned}M_1 &= M \pmod{p_1}, \\M_2 &= M \pmod{p_2}, \\&\vdots \\M_n &= M \pmod{p_n}, \\e_1 &= e \bmod (p_1-1), \\e_2 &= e \bmod (p_2-1), \\&\vdots \\e_n &= e \bmod (p_n-1)\end{aligned}$$

where e is a number relatively prime to $(p_1-1) \cdot (p_2-1) \cdot \dots \cdot (p_k-1)$,

$$Y_i = Y_{i-1} + [(M_i - Y_{i-1}) (w_i^{-1} \bmod p_i) \bmod p_i] \cdot w_i \bmod n$$

for $i \geq 2$ and

$$C = Y_k, \quad Y_1 = M_1, \quad \text{and} \quad w_i = \prod_{j < i} p_j.$$

15. The method according to claim 1, comprising the further step of:

decoding the ciphertext word signal C to the message word signal M, wherein said decoding step comprises the step of: transforming said ciphertext word signal C, whereby:

$$Y_i = Y_{i-1} + [(M_i - Y_{i-1}) (w_i^{-1} \bmod p_i) \bmod p_i] \cdot w_i \bmod n$$

where $i \geq 1$ and

$$M = Y_k, \quad Y_1 = C_1, \quad \text{and} \quad w_i = \prod_{j < i} p_j.$$

16. A cryptographic communications system comprising:
a communication medium;

an encoding means coupled to said communication medium and adapted for transforming a transmit message word signal M to a ciphertext word signal C and for transmitting C on said channel, where M corresponds to a number representative of a message and

$0 \leq M \leq n-1$ where n is a composite number of the form

$$n = p_1 \cdot p_2 \cdot \dots \cdot p_k$$

where k is an integer greater than 2 and p_1, p_2, \dots, p_k are distinct prime numbers, and where C corresponds to a number representative of an enciphered form of said message and corresponds to

$$C \equiv M^e \pmod{n}$$

where e is a number relatively prime to $\text{lcm}(p_1-1, p_2-1, \dots, p_k-1)$; and

a decoding means coupled to said communication medium and adapted for receiving C from said channel and for transforming C to a receive message word signal M' where M' corresponds to a number representative of a deciphered form of C and corresponds to

$$Y_i = Y_{i-1} + [(M_i / - Y_{i-1}) (w_i^{-1} \bmod p_i) \bmod p_i] \cdot w_i \bmod n$$

where $i \geq 1$ and

$$M = Y_k, \quad Y_1 = C_1, \quad \text{and} \quad w_i = \prod_{j < i} p_j.$$